Temporal changes of seismic velocities in the San Jacinto Fault zone associated with the 2016 $M_w 5.2$ Borrego Springs earthquake

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SUMMARY

We study temporal changes of seismic velocities associated with the 10 June 2016 $M_w 5.2$ Borrego Springs earthquake in the San Jacinto fault zone, using nine component Green’s function estimates reconstructed from daily cross correlations of ambient noise. The analysed data are recorded by stations in two dense linear arrays, at Dry Wash (DW) and Jackass Flat (JF), crossing the fault surface trace $\sim 3$ km northwest and southeast of the event epicentre. The two arrays have 9 and 12 stations each with instrument spacing of 25–100 m. Relative velocity changes ($\delta v/v$) are estimated from arrival time changes in the daily correlation coda waveforms compared to a reference stack. The obtained array-average $\delta v/v$ time-series exhibit changes associated with the Borrego Springs event, superposed with seasonal variations. The earthquake-related changes are characterized by a rapid coseismic velocity drop followed by a gradual recovery. This is consistently observed at both arrays using time- and frequency-domain $\delta v/v$ analyses with data from different components in various frequency bands. Larger changes at lower frequencies imply that the variations are not limited to the near surface material. A decreasing coseismic velocity reduction with coda wave lapse time indicates larger coseismic structural perturbations in the fault zone and near-fault environment compared to the surrounding rock. Observed larger changes at the DW array compared to the JF array possibly reflect the northwestward rupture directivity of the Borrego Springs earthquake.

Key words: Fault zone rheology; Coda waves; Seismic interferometry; Seismic noise; Wave scattering and diffraction.

1 INTRODUCTION

Co- and post-seismic temporal changes of seismic velocities associated with earthquakes of different sizes and in different tectonic settings have been studied using earthquake waveforms (e.g. Poupinet et al. 1984; Peng & Ben-Zion 2006; Sawazaki et al. 2009; Nakata & Snieder 2012; Roux & Ben-Zion 2013) and ambient noise cross correlations (e.g. Brenguier et al. 2008a, 2014; Froment et al. 2013; Obermann et al. 2014; Hobiger et al. 2016). Recent advances in deployments of dense seismic arrays around fault zones together with developments in analysis techniques provide improved opportunities to track temporal changes of seismic velocities in fault zone regions. The San Jacinto fault zone (SJFZ) is one of the most seismically active fault zones in southern California (e.g. Hauksson et al. 2012; Ross et al. 2017a; Ben-Zion & Zaliapin 2019), and is capable of producing large $M_w > 7.0$ earthquakes (e.g. Peterson & Wesnousky 1994; Onderdonk et al. 2013; Rockwell et al. 2015). Several $M_w > 5$ earthquakes occurred during the past decade in the complex trifurcation area of the SJFZ (Fig. 1a) associated with its three major fault branches, including the 2016 $M_w 5.2$ Borrego Springs (BS) earthquake with a hypocentre at $\sim 12$ km depth. Analysis of source properties of the 2016 BS event indicate that it had significant directivity to the northwest (Ross et al. 2017b). This inference is supported by the strongly asymmetric distribution of aftershocks of the BS event to the northwest of the main shock epicentre (Fig. 1).

Five linear arrays consisting of 6–12 stations with an average station spacing of $\sim 20–40$ m were deployed across different sections of the SJFZ (Vernon & Ben-Zion 2010). These include two arrays at Jackass Flat (JF) and Dry Wash (DW), which cross the main Clark branch of the SJFZ about 2–3 km to the northwest and southeast from the epicentre of the 2016 BS earthquake (Fig. 1). In this paper, we use ambient seismic noise recorded by these two linear arrays to analyse temporal changes of seismic velocities associated with the 2016 BS event. Regional tomographic images of the region (Allam & Ben-Zion 2012; Allam et al. 2014; Zigone et al. 2015; Fang et al. 2016) show a contrast of seismic velocities across the Clark fault with the southwest side being slower in the top few kilometres (background grey scale in Fig. 1a). Theoretical studies of bimaterial ruptures and the observed velocity contrast imply a likely preferred
Figure 1. (a) Map of the trifurcation area of the San Jacinto Fault Zone (SJFZ) and fault zone linear arrays (DW in green, JF in red) analysed in this study. The average P-wave velocity over the depth range 1–7 km based on tomographic results of Allam & Ben-Zion (2012) is shown as the background colour (grey—slow and white—fast). The blue star, beach ball and green arrow indicate the epicentre location, focal mechanism and rupture directivity of the 2016 Ms 5.2 Borrego Springs earthquake. Aftershocks detected and relocated by Ross et al. (2017a) are coloured by depth, whereas the green stars indicate Ms 3.0 + aftershocks. The regional background seismicity during 2015–2016 is denoted as black dots. Surface traces of the San Jacinto fault in the trifurcation area are shown as black lines. The top and bottom right insets contain the zoom in of the station configuration for the DW and JF arrays, respectively. (b) Depth section of hypocentres projected along the cross-section AA’ with aftershocks coloured by the time relative to the main shock (largest yellow star). The shaded grey area represents a region in which more than 0.5 m of slip occurred during the main shock according to Ross et al. (2017b). The Ms > 3 aftershocks are shown as stars scaled with respect to the corresponding magnitude, and the black dots indicate locations of the background seismicity occurred during 2015–2016. The green and red triangles denote the locations of JF and DW arrays, respectively.

propagation direction of earthquake ruptures in the area to the NW (e.g. Weertman 1980; Ben-Zion & Andrews 1998; Ampuero & Ben-Zion 2008) that is consistent with the observed directivity of the 2016 BS event. Fault zone imaging results at the JF and DW sites (Qiu et al. 2017a,b) suggest that both arrays cross the main seismogenic fault; however, the fault zone structures in the top few kilometres have different properties below the two arrays. Based on observation and modelling of fault zone trapped waves and delay time analysis of body waves, the JF array to the southeast of the BS event epicentre is situated in ∼200-m-wide fault damage zone with ∼35 per cent reduction of shear wave velocity relative to the host rock (Qiu et al. 2017a). In contrast, delay time analysis and lack of clear trapped waves indicate a more localized, that is considerably narrower than 200 m, fault zone structure at the DW array situated to the northwest (Qiu et al. 2017b). The configuration of two across-fault linear arrays at the opposite along-strike directions of the 2016 BS event epicentre provides a unique opportunity to investigate how the fault damage zone responds to a nearby moderate earthquake with rupture directivity.

Ambient noise correlation (ANC) techniques have been used extensively to image the subsurface between pairs of stations (e.g. Campillo & Paul 2003; Shapiro & Campillo 2004; Shapiro et al.
uous seismic records, transient signals generated by earthquakes almost symmetrically to each side of the epicentre of the 2016 BS period sensors. Both arrays with an aperture of consists of 9 broadband stations, and the DW array has 12 short-forms with 200 Hz sampling rate recorded by two linear fault zone We use 2 yr (2015–2016) of three-component continuous wave- 2 DATA AND PROCESSING

We use 2 yr (2015–2016) of three-component continuous wave- forms with 200 Hz sampling rate recorded by two linear fault zone arrays located in the trifurcation area of the SJFZ. The JF array consists of 9 broadband stations, and the DW array has 12 short-period sensors. Both arrays with an aperture of ~400 m are located almost symmetrically to each side of the epicentre of the 2016 BS earthquake (Fig. 1) and are capable of recording high quality ground motion from 0.1 to 10 Hz. The data from the JF array are analysed up to November of 2016 when the array was removed.

To retrieve high-quality Green’s function estimates from continu- ous seismic records, transient signals generated by earthquakes and other large episodic sources have to be removed prior to correlation (e.g. Bensen et al. 2007). To reduce computation time, we down sample the data to 40 Hz prior to the pre-processing. Here, we adopt the pre-processing procedure of Poli et al. (2012), Zigor et al. (2015) and Hillers et al. (2015a) to compute daily ANC. This includes large amplitude transients removal, spectral whitening and amplitude clamping. Trial and error analyses suggested an optimized preprocessing with a window length of 1-hr, 0.1–12 Hz frequency band for spectral whitening, and a thresh- old of 3.5 times the standard deviation in amplitude truncation. The 2016 BS event was followed by high rate of aftershocks that last for ~2 weeks (Fig. S1). Wavefield changes associated with small aftershocks (e.g. $M_w < 1.0$) within the first 2 weeks after the main shock are difficult to fully suppress and can bias the high-frequency Green’s function estimates (e.g. Obermann et al. 2015). Daily correlation functions of all station pairs within each fault zone linear array are computed by cross correlating the pre-processed data.

To achieve ANC with sufficient signal-to-noise ratio (SNR) and quality (Fig. 2), remaining low quality daily correlations are first removed from the raw correlation matrix (Fig. S2). Previous studies show that filtering (e.g. Hadzioannou et al. 2011; Stehly et al. 2015) and substacking at each date over a time interval of ±d days (e.g. Brenguier et al. 2008a) can increase the SNR of the correlation functions. In this paper, we use a Singular value de-composition (SVD) based Wiener filter (Moreau et al. 2017) to denoise the daily ANC matrix, which significantly improves the SNR of each individual daily trace. A 2-D low-pass SVD based Wiener filter with a size of 10 d and five samples (0.125 s) along the date and correlation lag time dimensions was found to yield the best results. The 10-d window size results in a 2–3 d temporal smoothing (e.g. Hillers et al. 2019). After these additional processing, we rotate the nine-component cross-reconstruction tensor into a system of fault perpendicular (R), along fault strike (T) and vertical directions (Z).

We then stack the filtered daily correlations from the first day of 2015 to the day of the year that is 1 month before the 2016 BS earthquake (green line in Figs 2a and b) to generate the reference waveform (Fig. 2c). Ending one month before the 2016 BS event is to guarantee that velocity perturbations caused by the main shock and aftershocks are not included in the reference, and to not erroneously associate potential changes at the end of the stack period to medium changes.

To determine the part of the reference waveform that is dominated by coda wave signals above the noise level—coda wave window, we investigate the energy decay as a function of lag time. We assume that, different from the amplitude of direct waves that is governed by both geometrical spreading and attenuation, the coda waves are only affected by intrinsic and scattering attenuation, whereas the base noise level should be independent of the lag time. We stabilize the estimates by averaging the envelope functions over all available station pairs for the ZZ component and analyse the median envelope. A complete description of the coda wave lag time am- plitude decay analysis can be found in the supplementary material (Appendix I and Fig. S3). Based on the fitting, the coda wave win- dows are $8 s \leq |\tau| \leq 40 s$ for 0.1–0.4 Hz, $8 s \leq |\tau| \leq 35 s$ for 0.5–2 Hz, $6 s \leq |\tau| \leq 23 s$ for 0.75–3 Hz, and $5 s \leq |\tau| \leq 22 s$ for 1–4 Hz. Here, we ignore the frequency band 0.25–1 Hz due to very low SNR levels (Fig. S4). Fig. S5 further validates that coherent coda arrivals can be extracted from ANC for frequency bands from 0.1–0.4 Hz up to 1–4 Hz within the determined coda wave window.
**Figure 2.** (a) Denoised daily ambient noise cross-correlations computed for year 2015 and 2016 between station pair JFS2 and JF00. The black dashed line indicates 10 June 2016, the origin time of the main shock, whereas the green line outlines the date one month before the main shock. Daily correlations below the green line are averaged to construct the reference trace shown in (c). The insets illustrate the zoom in of the reconstructed coda waves within the black boxes. (b) Same as (a) for station pair DW01–DW03. Obvious differences are observed in traveltimes of scattered arrivals before and after the main shock (black dashed lines). (c) Reference waveforms computed at station pairs JFS2–JF00 (black) and DW01–DW03 (blue). Coda waves between correlation times of 6 and 40 s (dashed black boxes) are zoomed in the insets. The red dashed boxes in the insets indicate the correlation time range used to plot the insets in (a) and (b).

### 3 METHODOLOGY

#### 3.1 Relative velocity change estimates

For a scattered arrival reconstructed from ANC, let $t$ be the absolute traveltime observed in the reference trace and $\delta t$ denotes the difference in traveltime measured between an instance of a daily correlation and the reference. The relative velocity change ($\delta v/v$) is given by the relationship (e.g. Ratdomopurbo & Poupinet 1995; Snieder et al. 2002)

$$
\frac{\delta v}{v} = -\frac{\delta t}{t}.
$$

Instead of using individual scattered arrivals, a coda wave window is commonly used to stabilize the estimate. Since scattered arrivals with greater traveltime $t$ have a correspondingly longer propagation path, the resulting estimations represent velocity perturbations averaged over larger areas surrounding the interstation path. Assuming a homogeneous relative velocity change, the obtained $\delta v/v$ can be interpreted as the perturbation in medium properties for the sampled region.

We use the time-domain stretching method (Lobkis & Weaver 2003) and the frequency-domain doublet method (e.g. Poupinet et al. 1984) to estimate $\delta t/t$ from coda waves. Both methods compare a test trace to a reference trace and assume that temporal perturbations in coda wave traveltimes are small. The stretching method dilates or compresses coda waveforms in time domain, whereas the doublet method uses the moving window cross-spectral analysis (Clarke et al. 2011) to estimate $\delta v/v$.

Both methods have their advantages and disadvantages. Spurious velocity change estimates may be observed using the stretching method when the coda wave amplitude spectrum varies with time (Zhan et al. 2013). However, the time-domain technique processes the whole coda waveform at once and was found to yield more stable and precise estimation of $\delta v/v$ with noisy data (e.g. Sens-Schönfelder & Larose 2008; Hadziioannou et al. 2009). In contrast, the phase-based estimates of the doublet method are not affected by variations in the noise amplitude spectrum (Hadziioannou et al. 2009; Colombi et al. 2014). The frequency-domain method, on the other hand, suffers from problems such as cycle skipping (Mikesell et al. 2015), in which phases are matched incorrectly between the
coda waves in the test and reference traces, and the tradeoff between the Fourier transform window length and the accuracy of the \( \delta v/v \) measurement (Hadziioannou et al. 2011). Since these two methods behave differently in the presence of fluctuations, consistency between estimations obtained from both techniques is indicative of the robustness of the resulting \( \delta v/v \).

Noise recorded in the SJFZ environment is excited by different mechanisms: microseisms from ocean-continent interactions in the low-frequency band 0.1–0.4 Hz, and other natural and cultural sources (Hillers & Ben-Zion 2011; Inbal et al. 2018) for higher frequencies (e.g. >1 Hz). Although the noise sources are not evenly distributed for frequencies above 0.1 Hz in the study region (e.g. Hillers et al. 2013), the amplitudes of coda waves are similar at different time lags for all the frequency bands (Fig. S5). The coda waves are less symmetric in shape at frequencies above 0.5 Hz (e.g. Figs S5c–f). To minimize the effect of non-isotopic noise sources, we use the coda waves from both positive and negative time lags simultaneously to determine \( \delta v/v \).

In contrast to previous studies using networks with apertures of tens of metres to hundreds of kilometres, the linear arrays analyzed here are situated within fault damage zones that may yield larger temporal changes compared to the surrounding rock. For such localized temporal changes in rock properties, \( \delta v/v \) tends to be larger at early scattered arrivals and decreases with lapse time (e.g. Obermann et al. 2016), because coda waves arriving at later lapse times averaged the seismic velocity variations over a larger area including host rock regions that are less affected compared to the near fault material. As a result, the underlying assumption of the doublet method that \( \delta v/v \) is independent of the lapse time \( t \) can be estimated through linear regression using moving window is not fully compatible with the observation. The stretching method, on the other hand, provides estimates using the optimally dilated waveforms, which are dominated by large amplitude coda waves at early correlation time (Fig. S3).

### 3.2 Curve fitting

Fig. 3 shows example time-series of \( \delta v/v \) and corresponding coherence estimates \( C_{\max, \delta v/v} \) at 1–4 Hz using both the stretching and doublet methods at the DW and JF arrays. The coherence value provides an estimate of the similarity between the two compared time-series. In this section, we model the obtained \( \delta v/v \) time-series considering three main components: a long-term linear trend, quasi-periodic variations and coseismic velocity reduction followed by a recovery process associated with the 2016 BS earthquake. To quantify these components, we approximate the \( \delta v/v \) time-series with the following parametrization:

\[
f(T) = f_{\text{lin}}(T) + f_{\text{eq}}(T - T_0) + f_{\text{pet}}(T),
\]

(2)

where \( T \) is the number of days from the first day of analysis period (2015-01-01) and \( T_0 \) is the origin time of the 2016 BS event. A long-term linear trend in \( \delta v/v \) time-series has been observed in previous studies (e.g. Fig. 3 of Hillers et al. 2015a; Taira et al. 2018) and is often attributed to long-term variations of the subsurface water content. Interpretation of linear trends is outside the scope of this study, but adding a linear term \( f_{\text{lin}} \) to eq. (2), which is equivalent to detrending the \( \delta v/v \) time-series, can improve the fitting results so this is included in the analysis.

The second term in eq. (2), \( f_{\text{eq}} \), represents the co- and post-seismic velocity changes, which are the main focus of this study, and can be approximated by a Heaviside step function \( H(T) \) combined with a logarithmic recovery:

\[
f_{\text{eq}}(T) = -E_1 \cdot H(T) + E_2 \cdot \ln(1 + T) \cdot H(T),
\]

(3)

where \( E_1 \) represents the coseismic velocity reduction and \( E_2/E_1 \) constrains the post-seismic recovery time (Fig. S9a). Eq. (3) is similar to the expression used by Hobiger et al. (2012) with added 1 to regularize the log function near zero time. Laboratory data indicate that log(t) healing already operates at 1 s after failure (e.g. Nakatani & Scholz 2004). Since the minimum timescale in the performed analysis is 1 d (=8.6 × 10^4 s), and the examined post-seismic period includes only about 6 months, the results do not resolve the first 10^4 to 10^6 s of the healing process and do not include sufficient long time intervals (in log scale) to resolve the later post-seismic recovery. Furthermore, a logarithmic post-seismic recovery can exceed at long time the pre-seismic velocity level (e.g. green and blue curves in Fig. S9a), which is not physical. In this case, it is convenient and numerically more stable to utilize an exponential function to model the post-seismic \( \delta v/v \), and derive an effective recovery timescale based on that function (Hobiger et al. 2014; Fig. S9b). Given the fluctuating character of the results (Fig. 3) and the short duration of the available data, we use a simple exponential function to approximate the post-seismic recovery (Taira et al. 2018; Fig. S6b):

\[
f_{\text{eq}}(T) = -E \cdot H(T) \cdot e^{-T/T_\varepsilon},
\]

(4a)

where \( E \) and \( T_\varepsilon \) represent the resolved coseismic velocity reduction and post-seismic recovery time.

The time resolution of the resulting \( \delta v/v \) curve is limited by the denoising filter (Moreau et al. 2017), low quality daily ANC that are removed in the pre-processing steps (i.e. missing data points), and using the median of measurements obtained from all station pairs within an array. The stars in Fig. 3 outline a period, referred to below as the ‘coseismic period’. The shaded area is magnified in the insets and illustrates such smoothing effects. The maximum coseismic velocity reduction of the smoothed time-series (blue curves in bottom panels of Fig. 3) are not well aligned with the occurrence time of the 2016 BS event (red dashed lines). In addition, instead of a rapid drop, the coseismic velocity decreases rather gradually within the shaded time interval. The coseismic period is generally longer for DW array than that of JF array (Figs 3 and S6–S8), as recordings at the JF site are less affected by the aftershocks (coloured circles in Fig. 1).

Due to the averaging effects of \( \delta v/v \) curve in the coseismic period, we estimate \( E \), the coseismic velocity reduction, directly from the time-series instead of including it in the curve fitting. First, we measure the difference between the maximum—\( f_{\text{max}} \) (at \( T = T_1 \); e.g. white star in Fig. 3) and minimum—\( f_{\text{min}} \) (at \( T = T_2 \); e.g. red star in Fig. 3) values of the \( \delta v/v \) curve 10 d before and 20 d after the 2016 BS event (shaded area in Figs 3 and S6–S8). Then, we can rewrite eq. (4a) as

\[
f_{\text{eq}}(T) = -(f_{\text{max}} - f_{\text{min}}) \cdot H(T) \cdot e^{-T/T_\varepsilon},
\]

(4b)

where \( E = f_{\text{max}} - f_{\text{min}} \). Moreover, we exclude \( \delta v/v \) measurements within the coseismic period (i.e. \( T_1 \leq T \leq T_2 \)) from the curve fitting.

Non-recovering velocity reductions after large earthquakes caused by material damage have been observed and modelled in previous studies (e.g. Peng & Ben-Zion 2006; Hobiger et al. 2016). A complete post-seismic recovery is observed within ~1 month after the 2016 BS event at 0.1–0.4 Hz (Fig. S6). However, at frequencies above 0.5 Hz, the obtained \( \delta v/v \) curves are not fully recovered due to insufficient long acquisition of seismic data after the BS.
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Figure 3. Coherence and δv/v time-series obtained for (a) DW array using stretching method, (b) DW array using doublet method, (c) JF array using stretching method, and (d) JF array using doublet method. The grey curve represents the coherence (top panel) and δv/v (bottom panel) for each station pair. The blue solid and dashed curves denote the array-median and corresponding uncertainty calculated using results from all the station pairs. The stars denote the beginning and end of the coseismic period (Section 3.2). Measurements within the shaded area are magnified and shown in the inset. Coda waves from ZZ component within the coda wave window (i.e. 5–22 s; Fig. S3d) bandpass filtered at 1–4 Hz are used. The red and black dashed lines mark the origin time of the 2016 BS earthquake and the end of the stacking range used to construct the reference waveform, respectively.

For $f_{\text{per}}$ in eq. (2), we only include annual variations (e.g. Hillers et al. 2015a) in the curve fitting:

$$f_{\text{per}}(T) = C \cdot \cos \left[ \omega (T - T_\omega) \right],$$

with $C$ being the amplitude. $\omega$ is a fixed value of $2\pi$/year, and $T_\omega$ is the initial phase of the annual variation. Since the curve fitting results are already sufficiently good using eq. (5) (Fig. 4), we do not include a semi-annual (e.g. Johnson et al. 2017) term here.

We estimate $C$, $T_\omega$, and $T_\omega$ in eqs (2), (4b) and (5), and the corresponding uncertainties, for each array-median $\delta v/v$, using a non-linear least square curve fitting algorithm from the SciPy package (e.g. Figs 4 and 5). Uncertainty of the array-median $\delta v/v$ is computed as the standard deviation of the median (blue dashed curves in Fig. 3) and utilized to determine the weight of an estimate in curve fitting. The best-fitting linear trend ($f_{\text{lin}}$) and seasonal variations ($f_{\text{per}}$) are subtracted from the obtained $\delta v/v$ to highlight the co- and post-seismic responses. Considering the fluctuations in $\delta v/v$ obtained from different station pairs (e.g. grey curves in Fig. 3) and limited data for the post-seismic period, the purpose of the curve fitting is to provide first order estimates for the phase and amplitude of seasonal variations (Section 4.1.1), coseismic velocity reduction (Section 4.1.2) and post-seismic recovery time (Section 4.1.3). For a more precise analysis of coseismic and post-seismic components, $\delta v/v$ curves after removing the modelled long-term variations (i.e. $f_{\text{lin}}$ and $f_{\text{per}}$) are examined in Section 4.2.

4 RESULTS

Fig. 3 shows the resulting $\delta v/v$ obtained from ZZ correlations filtered at 1–4 Hz using coda waves in the time window of 5–22 s (see Figs S6–S8 for other frequency bands). Results of $\delta v/v$ from the stretching (Figs 3a and c) and doublet (Figs 3b and d) methods show the same systematic temporal patterns. The results differ in the coherence values (lower for the doublet method)
and in the amplitudes of the $\delta v/v$ variations and the corresponding uncertainties. Systematic higher coherence values from the stretching method reflect the comparison of optimally dilated waveforms. Results from the doublet method used for comparison with the stretching method are shown in the supplementary materials.

Considering the small aperture (∼400 m) of the two fault zone arrays, the purpose of this section is to use the array-median $\delta v/v$ time-series to infer a robust estimation of the seismic velocity perturbation in the fault damage zone, and analyse relations of the observed temporal patterns with the 2016 BS event and other natural loads that can be driven by temperature variations. While averaging $\delta v/v$ time-series for the entire array suppresses the background variations, the array-median $\delta v/v$ curve may yield less sharp coseismic velocity reduction. This is because the background fluctuation in $\delta v/v$ varies in phase for different station pairs, so any rapid changes tend to be averaged over time. In addition, similar to the Fréchet kernel for finite frequency traveltimes (e.g. Dahlen et al. 2000), the sampled volume and thus the sensitivity of coda waves to velocity perturbations in a heterogeneous medium increases both horizontally and vertically with lapse time (e.g. Obermann et al. 2013, 2016). The sensitivity halo for coda waves thus likely exceeds the size of the ∼200 m wide fault damage zone, particularly at low frequencies (e.g. 0.1–0.4 Hz) and longer lapse time (e.g. 30–40 s). A detailed study of $\delta v/v$ measured for coda waves at different lapse times (Section 4.2.1) can provide constraint on rock susceptibility to perturbations in fault damage zones and the surrounding rock.

### 4.1 Results of curve fitting

Fig. 4 illustrates the curve fitting results of the array median $\delta v/v$ time-series estimated for the DW array using the stretching method (see Fig. S10 for the doublet method; Figs S11, S12 for the JF array). ZZ component correlations and the frequency dependent coda wave windows shown in Fig. S3 are used here. The best-fitting parameters, amplitude ($C$) and phase term ($T_\omega$) of seasonal components, post-seismic recovery time ($T_c$) and the measured coseismic velocity reduction ($E$) are indicated in the figure. The measurements for all the frequency bands, arrays, components and lapse time windows are well quantified by the modelled $\delta v/v$ time-series. The fitness generally increases with frequency. In this section, we mainly focus on the best-fitting parameters shown in Fig. 5.

At 0.1–0.4 Hz, we find large amplitude periodic (30–40 d periodicity) fluctuations in $\delta v/v$ between June and October of 2015 (e.g. Fig. 4a), particularly at the DW array. Peak-to-peak amplitude of the oscillation is comparable to the observed coseismic reduction in $\delta v/v$ for both arrays. Based on the earthquake catalogue of Hauksson et al. (2012, updated to later years at the SCEDC 2013), there are no $M_w > 3.0$ earthquakes in the study region (Fig. 1a) between June and October of 2015. This large-amplitude transient fluctuation correlates well with the visible waveform perturbations in daily ANC computed for the station pair DW01–DW03 (Fig. 2b, between day of the year 100 and 300) and is responsible for the poor estimation of the seasonal variations (Fig. 4a). However, we do not observe fluctuations on that
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4.1.1 Seasonal variations—parameters $C$ and $T_w$

The annual variation term $f_{\text{per}}$ is characterized by the amplitude $C$ and peak time $T_w$. Best-fitting values of $C$ (0.03–1 per cent) and $T_w$ (150–330 d) estimated from the DW and JF arrays using both methods are shown in Figs 5(a) and (b), respectively.

There are two broad possible causes for the derived seasonal variations in seismic velocities: changes in medium properties, such as crack density or fluid content, and variations caused by wavefield properties that are considered spurious (Zhan et al. 2013). To identify the dominant driving mechanism for seasonal variations in the SJFZ, Hillers et al. (2015a) performed lapse time analysis and investigated the delay between the obtained seasonal variations and various relevant environmental records such as atmospheric temperature, wind speed and precipitation. They concluded that the $\delta \nu/\nu$ variations in the SJFZ at 0.1–0.4 Hz are likely caused by wavefield changes. For the frequency ranges of 0.5–2 and 1–4 Hz, however, the results more likely reflect the medium response and the most plausible primary mechanism was inferred to be thermoelastic strain (e.g. Berger 1975; Ben-Zion & Leary 1986). We also perform lapse time analysis and show corresponding results in Figs S13 and S14. To clarify the primary mechanism, we examine the delay between the observed seasonal variations and annual air temperature. The surface temperature record is taken from the Piñon Flats observatory near the SJFZ (Hillers et al. 2015a) and it reaches the maximum around day 200 of the year. Therefore, we use $T_{\text{max}} = 200$ (dashed black lines in Fig. 5b) as the peak time of the annual surface temperature for both array locations to roughly estimate the delay between the $\delta \nu/\nu$ signals and the air temperature.

At the low-frequency band 0.1–0.4 Hz, we find large deviations between $C$ values (eq. 5) based on different methods (circles versus triangles in Fig. 5a) or arrays (red versus blue in Fig. 5a). The differences in $C$ values derived from the stretching and doublet methods indicate that the seasonal signals extracted from time- and frequency-domain are inconsistent. The systematic larger $C$ value at DW array may reflect differences in array configurations and in situ conditions between the two arrays. In addition, the $C$ values at 0.1–0.4 Hz yield significantly larger seasonal variations compared to the analysed higher frequency bands (Fig. 5a). On the other hand, very similar $T_w$ values (eq. 5) are obtained at the low-frequency band for both methods (Fig. 5b): the seasonal variations peak at $T_w \approx 200$ and 150 for the DW and JF arrays, respectively. The fact that the obtained $T_w$ values are equal or smaller than $T_{\text{max}}$ (i.e. 200) rules out thermoelastic strain as the dominant mechanism for
Considering the potential biases in estimates of the absolute coseismic velocity reduction \(E\), due to variations in the noise wavefield properties associated with the aftershock activity, we compare \(E\) values derived from different methods. At the low frequency band 0.1–0.4 Hz, the \(E\) estimated from the stretching method-based \(\delta v/v\) time-series is \(\sim 2\) times as large as that of the doublet method-based results for both arrays. The values of \(E\) are \(> 3\) per cent at DW array and between 0.3 and 1.3 per cent at the JF array (Fig. 5c). Our results are much larger (\(> 10\) times) than that resolved at Parkfield between 0.1 and 0.9 Hz (\(< 0.1\) per cent; Bronguier et al. 2008a). At frequency bands between 0.5 and 4 Hz, the \(E\) value is \(\sim 0.15–0.35\) per cent for both arrays and methods (Fig. 5c). Our \(> 0.2\) per cent coseismic velocity reduction is comparable to those observed in fault zone environments in Japan and in the Salton Sea geothermal field between 0.5 and 4 Hz (Hobiger et al. 2016; Taira et al. 2018). These comparisons indicate that the coseismic changes in velocities occur mainly near faults at low frequencies (0.1–0.4 Hz) but are not limited to fault zone materials at higher frequencies (>0.5 Hz).

4.1.3 Post-seismic velocity recovery—parameter \(T_c\)

In Section 3.2, we modelled the post-seismic velocity recovery using an exponential function (eq. 4a), as the logarithmic function (eq. 3) suffers from an overshooting issue (Fig. S6) in curve fitting. The characteristic time \(T_c\) (eq. 4a) quantifies the post-seismic response with a larger value indicating a slower recovery. As discussed in Section 2, we have less than 6 month of data to constrain the post-seismic \(\delta v/v\). When the time for a complete post-seismic recovery is longer than 6 months (i.e. \(\sim 180\) d), \(T_c\) could not be well constrained through curve fitting and often yields a large discrepancy between results from the stretching and doublet methods (Fig. 5d). In addition, the accuracy of the estimated post-seismic recovery time \(T_c\) also depends significantly on the quality of the estimation for the coseismic velocity reduction \(E\), which is not well constrained for the DW array results due to a 2-week-long background oscillation immediately after the BS event. In general, both stretching and doublet methods show compatible trends in Fig. 5(d).

At the low frequency band 0.1–0.4 Hz, \(T_c\) is \(\sim 10\) d for both arrays and methods. However, \(T_c\) estimates at the higher frequency bands are much larger. At the JF array, both methods suggest \(T_c\) \(\approx 150\) d from 0.5–2 Hz to 1–4 Hz. At the DW array, \(T_c\) values (\(\sim 200–300\) d) are larger than those of JF array for both methods.

Considering post-seismic \(\delta v/v\) curve at 0.1–0.4 Hz are poorly fitted based on eq. (4a) (Fig. 4a and S10a), we refine the post-seismic analysis using a logarithmic function (eq. 3). Different from an exponential post-seismic process (eq. 4a) that requires an infinite long time for a complete recovery, the time of a complete post-seismic recovery, characterized by a logarithmic function, is given by \(T_{\text{log}} = e^{E_1/E_2} - 1\) (eq. 3). To fit the \(\delta v/v\) curve with eq. (3), we first remove the best-fitting long-term variations; \(f_{\text{lin}}\) and \(f_{\text{pe}}\) estimated in Section 3.2 from the obtained \(\delta v/v\) curve—\(f_{\text{obs}}\) to highlight the co- and post-seismic responses:

\[
\hat{f}_\text{eq}(T - T_0) = f_{\text{obs}}(T) - f_{\text{lin}}(T) - f_{\text{pe}}(T).
\] (6)

We then fit the corrected \(\delta v/v\) measurements—\(\hat{f}_\text{eq}\) in a specific post-seismic time window \((T_p < T < T_{\text{pe}})\) with eq. (3), which is equivalent to the linear regression of \(\hat{f}_\text{eq}(T) - T_0\) on \(\ln(1 + T - T_0)\). Note that the estimates of \(E_1\) and \(E_2\) can be sensitive to the selection of the post-seismic window, particularly for cases with insufficient long records (Fig. S15; frequencies >0.5 Hz).
Therefore, we only discuss the results of this logarithmic post-seismic analysis for the frequency band 0.1–0.4 Hz, where a complete recovery is achieved in the obtained $\delta v/v$ curve and is poorly fitted using an exponential function (e.g. Fig. 4a).

Fig. 6 shows the best-fitting logarithmic post-seismic recovery and corresponding estimates of coseismic velocity reduction $E_{\text{log}}$ (i.e. $E_1$) and post-seismic recovery time $T_{\text{log}}$. A complete description of the determination of the time window used in the analysis can be found in the supplementary material (Appendix II). In general, $\int_0^\infty (T - T_0) E_{\text{log}}$ in the selected post-seismic window (grey dots within the black dashed lines in Fig. 6) yields a good agreement with the assumed logarithmic recovery (straight red dashed lines in Fig. 6). Since a complete recovery (blue dashed lines in Fig. 6) is achieved, $T_{\text{log}}$ is well constrained (∼30 d) for both arrays and methods at 0.1–0.4 Hz.

The estimated coseismic velocity reduction $E_{\text{log}}$, however, is much larger than $E$ estimated in Section 3.2, particularly at the DW array (e.g. $E \approx 6$ per cent in Fig. 4a and $E_{\text{log}} \approx 36$ per cent in Fig. 6a). This is because the coseismic velocity drop obtained from the $\delta v/v$ curves is largest at 5–14 d after the BS event due to limitations in the time resolution (Section 3.2) and thus includes a partial recovery, whereas the refined fitting with the logarithmic function includes information on earlier parts of the recovery process and thus yields much larger total coseismic velocity changes. The estimates of $E_{\text{log}}$ are based on the assumption of a constant rate of logarithmic recovery (i.e. $E_2/E_1$; e.g. slope of dashed red lines in Fig. 6). $E_{\text{log}}$ can be even larger if the actual recovery is much faster at the early 2 weeks of the post-seismic period ($T \leq 14$ d) than that indicated by measurements in the period of $T > 15$ d (dashed lines in Fig. 6).

### 4.2 Comparative analyses

In Section 4.1, the curve fitting results provide first order estimates of different components of the observed $\delta v/v$ time-series. Best-fitting parameters achieved from different methods and frequency bands are compared, indicating robust co- and post-seismic responses associated with medium changes caused by the 2016 BS earthquake. In this section, we remove the modelled linear trend and seasonal variations (eq. 6) to highlight the earthquake related variations (i.e. EQ responses) in the observed $\delta v/v$.

#### 4.2.1 Lapse time analysis

To analyse potential localized distribution of temporal changes of rock properties, $\delta v/v$ is estimated as a function of lapse time $\tau$ using small moving windows of coda waves. Fig. 7 compares the EQ responses of $\delta v/v$ and corresponding coherence estimates obtained using the stretching method. Several 10s-long moving time windows within the coda wave window are used. We use frequency bands 0.1–0.4 Hz and 1–4 Hz for the lapse time analysis as these results are clearest. In general, we observe very high consistency in co- and post-seismic responses from results for all lapse time windows. However, the coseismic velocity reduction decreases monotonically with lapse time of the moving window. Similar patterns are observed in results obtained using the doublet method (not shown here).

To further investigate the rate of decrease in the coseismic reduction with lapse time, we analyse the coseismic medium changes as a function of lapse time in Figs 8(a) and (b). Here we approximate the coseismic velocity reduction as the differences between the maximum and minimum $\delta v/v$ values (e.g. stars in Fig. 3) within the coseismic period (shaded area in Fig. 3). For the low-frequency band 0.1–0.4 Hz, the rate at which the coseismic $\delta v/v$ decreases with lapse time is much higher at DW than JF array, particularly at early lapse times. The rate is approximately the same for both arrays at 1–4 Hz. Coherence values, on the other hand, generally decrease with lapse time (Figs 8c and d) in both frequency bands, because of smaller SNR for coda waves at later lapse time (Fig. S3).

We also compare the post-seismic recovery rate obtained for different lapse times. The coseismic velocity reduction is fully recovered with ∼30 d after the 2016 BS event for all lapse times at 0.1–0.4 Hz (Figs 7a and b). This rapid recovery likely reflects the faster post-seismic healing process in fault damage zones due to larger normal stress at greater depth. In general, we expect the fault damage zone to have a different healing rate compared to the surrounding host rock. However, the post-seismic $\delta v/v$ yield the same recovery time for all lapse times (Figs 7a and b), despite the fact that coseismic velocity reduction ($E$) decreases with lapse time (Fig. 8a), which may indicate the coseismic velocity changes in the surrounding host rock are negligible compared to those within the fault damage zone at 0.1–0.4 Hz. At 1–4 Hz, the coseismic reduction is not fully recovered due to the limited period of recording (Figs 7e, d). The longer recovery time at higher frequency is also consistent with the smaller normal stress at shallower depth that delays the post-seismic healing process. In addition, we find the post-seismic $\delta v/v$ recovers faster at earlier lapse time for the first 3–4 months after the 2016 BS event in Fig. 7(c). As $\delta v/v$ at later lapse time are more sensitive to larger area, this observation at DW array may reflect a faster healing process close to fault damage zone during the first few months of the post-seismic period.

#### 4.2.2 Frequency band

Fig. 9 shows the comparison of the EQ responses estimated at different frequency bands for both DW and JF arrays. The coseismic velocity reduction and post-seismic recovery at 0.1–0.4 Hz are significantly larger and faster than those at frequencies above 0.5 Hz, respectively. To estimate the depth range of the observed frequency dependent coseismic $\delta v/v$ reduction, we need to consider the sensitivity of coda waves to local medium changes at depth. The coda is a mixture of body and surface waves in most crustal-like materials, and the partitioning between their contributions to the coda sensitivity depends on the heterogeneity of the medium and the coda lapse time (e.g. Obermann et al. 2013, 2016). For a first-order estimation, we ignore the contribution of body-wave sensitivity and assume the observed $\delta v/v$ are most sensitive to medium changes at a depth of $h_{\text{max}}$ that is proportional to the dominating wavelength $\lambda$.

We set $h_{\text{max}} = \lambda/3$ based on the depth sensitivity of surface wave phase velocity to shear wave velocity (e.g. Zigone et al. 2015; Berg et al. 2018). This relation suggests coda waves at lower frequency are more sensitive to changes in deeper structures. In this section, we provide a rough estimation on the depth of coseismic medium changes based on the surface wave depth sensitivity kernel and validate the assumption that the coseismic $\delta v/v$ observed at lower frequencies are representative to seismic velocity perturbations in deeper structures.

At 0.1–0.4 Hz, the dominating frequency, $f$, is ∼0.14 Hz (secondary microseism), and the corresponding phase speeds, $c$, in fault damage zones at the DW and JF sites (e.g. Roux & Ben-Zion 2017; Berg et al. 2018) are ∼3.2 km s$^{-1}$ for Rayleigh wave (e.g. ZZ component) and ∼3.4 km s$^{-1}$ for Love wave (e.g. TT component).
Figure 6. (a) EQ responses of $\delta V/V$ curve (eq. 6) after the origin time of the 2016 BS earthquake ($T > T_0$) at 0.1–0.4 Hz for DW array shown as a function of $\ln(1 + T - T_0)$. The dashed lines outline the portion of data that show a clear logarithmic recovery (red dashed lines) and is used to estimate the coseismic velocity reduction $E_{\log} (= E_1)$ and post-seismic velocity recovery time $T_{\log} (= e^{E_1/E_2} - 1; eq. 3)$. The horizontal blue dashed lines denote $\delta V/V = 0$. (b) Same as (a) for doublet method-based results. (c) Same as (a) for JF array. (d) Same as (b) for JF array.

Therefore, the apparent $\delta V/V$ is most sensitive to medium changes at the depth of $h_{\text{max}} = \lambda/3 = c/3f$, which is $\sim 7$–$8$ km. Similarly, for frequency bands above 0.5 Hz (i.e. $f > 0.5$ Hz), $h_{\text{max}}$ is smaller than 2 km as $c < 3$ km s$^{-1}$ (Qiu et al. 2019). Yang et al. (2019) found significant effects of shallow seismic velocity changes on phase velocities also of long periods (e.g. > 15 s) surface waves. Therefore, one cannot simply project the observed $\delta V/V$ at a low frequency band (e.g. 0.1–0.4 Hz) to deeper structure without considering the measurements at higher frequency bands (e.g. 1–4 Hz). However, we observe that the largest coseismic velocity reduction (>0.5 per cent) followed by a significantly faster post-seismic recovery at the low-frequency band 0.1–0.4 Hz (Figs 5c and d). This implies that the observed coseismic velocity reduction at the low-frequency band is not significantly biased by medium changes in the shallow structure.

4.2.3 Different components

The recording component is indicative of the type of surface wave (e.g. ZZ—Rayleigh wave and TT—Love wave) reconstructed from ANC. The coda, however, is a mixture of scattered body and surface waves and thus does not have a simple relation between waveforms recorded at different components.

Fig. 10 illustrates the EQ responses estimated at different components using the stretching method for DW array (Fig. S16 for doublet method; Figs S17, S18 for JF array). Except for the low frequency RT and ZT results, we observe generally similar rapid coseismic velocity reductions followed by a post-seismic recovery associated with the 2016 BS earthquake for all components in each frequency band. Although the results include some variations in co- and post-seismic responses estimated at different components, there is no clear component-related pattern that can be easily interpreted. In general, the results obtained from different components indicate higher similarity at frequencies above 0.5 Hz than that at the 0.1–0.4 Hz. This is understood to result from coda waves at high frequencies contain high degree of mixing modes, that is multiple scattering, whereas the mixing is not as complete at the low-frequency band (Hillers et al. 2013), due to the proximity of the study area to excitation region and the requirement of longer mean free path.

4.2.4 Array location

The observed $\delta V/V$ time-series is determined by the loading mechanism and magnitude, and properties of the local structures like rock susceptibility beneath the stations. To compare the magnitude of coseismic loadings at the DW and JF sites, we remove effects of local structures in the observed coseismic $\delta V/V$. Since both arrays are located in fault damage zones with similar array geometry (insets in Fig. 1) and the inter-array distance is only $\sim 6$ km, we assume that the amplitude of seasonal variations ($C$), either governed by medium or wavefield changes, is the same if the local conditions are similar at both sites. In other words, the observed $C$ value is a first order proxy for the susceptibility of the fault damage zone,
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Figure 7. (a) Array-median coherence (top panels) and $\delta v/v$ curves (bottom panels) measured using different lapse time windows (coloured curves) at 0.1–0.4 Hz. Model predicted linear trend and quasi-periodic components are removed from the $\delta v/v$ curves (eq. 6). (b) Same as (a) for JF array at 0.1–0.4 Hz. (c) Same as (a) for DW array at 1–4 Hz. (d) Same as (a) for JF array at 1–4 Hz.

Figure 8. Lapse-time dependent coseismic velocity reduction and median coherence values derived from curves shown in Fig. 7. (a) Coseismic velocity reduction measured at 0.1–0.4 Hz as a function of lapse time window. Results for DW and JF array are shown in red and blue, respectively. (b) Same as (a) for 1–4 Hz. (c) Same as (a) for coherence values. (d) Same as (c) for 1–4 Hz.
that is larger $C$ value indicates material that is more susceptible to changes. Although the peak time $T_0$ of seasonal variations is different between two arrays, the discrepancy is associated with the phase and thus has less effect on the rock susceptibility. Therefore, we normalize the $\delta v/v$ time-series by the corresponding best-fitting $C$ value to account for local response.

**Figure 10.** Comparison of the smoothed EQ responses of $\delta v/v$ measured using different components (colours) for DW array and stretching method at frequency bands (a) 0.1–0.4 Hz, (b) 0.5–2 Hz, (c) 0.75–3 Hz and (d) 1–4 Hz.

Fig. 11 compares the normalized EQ responses for the DW (blue in Fig. 11) and JF (red in Fig. 11) arrays at 1–4 Hz. The top and bottom panels represent results using the stretching and doublet methods, respectively. Systematically larger coseismic reductions are observed at DW compared to those at JF for both methods and all three analysed components. The same pattern is also ob-

**Figure 9.** Comparison of the EQ responses of $\delta v/v$ measured at four different frequency bands (colours) for the DW (left-hand panel) and JF (right-hand panel) arrays. ZZ component and stretching method are used. Median filter is applied to suppress the background fluctuations (transparent curves). The smoothed $\delta v/v$ time-series are shown as solid curves. The right $y$-axis in red denotes the scale of the red curves (0.1–0.4 Hz).
Figure 11. Comparison of the normalized EQ responses of $\delta v/v$ measured at 1–4 Hz for the DW (red) and JF (blue) arrays. (a) The thin and thick curves represent the normalized raw and smoothed array-median $\delta v/v$, respectively. Results obtained from stretching method and ZZ component are used. Each $\delta v/v$ curve is normalized by its corresponding best-fitting $C$ value (seasonal variation amplitude; Fig. 3a). (b) Same as (a) for RR (fault perpendicular) component. (c) Same as (a) for TT (fault parallel) component. (d), (e), (f) same as (a), (b), (c) for doublet method.

served at the low frequency band 0.1–0.4 Hz (Fig. S19), but less clear at 0.5–2 Hz (Fig. S20) and 0.75–3 Hz (Fig. S21). Since the effects of site-specific structures are reduced, this observation suggests that the difference is associated with the NW rupture directivity of the 2016 BS earthquake (Fig. 1a) and the resulting larger amplitudes of seismic waves propagating towards the DW array.

5 DISCUSSION AND CONCLUSIONS

We monitor seismic velocity changes in the San Jacinto fault zone for a 2-year period (2015–2016) using ambient seismic noise recorded by two linear arrays with an aperture of ~400 m. The two arrays at sites DW and JF are located within fault damage zones (Qiu et al. 2017a,b) at ~3 km distance to the NW and SE of the 2016 $M_w$ 5.2 Borrego Springs earthquake. Relative velocity changes ($\delta v/v$) are estimated using a time- and a frequency-domain method. Results from both methods are compared to distinguish medium changes from spurious variations. Clear seasonal variations and co- and post-seismic changes associated with the BS event are observed in the obtained $\delta v/v$ time-series. A decreasing signal is often seen in the $\delta v/v$ curve several days before the BS event (e.g. Figs 7a and d); this is not interpreted as a precursor signal as the trend is likely associated with the choice of the reference period (black dashed lines in Fig. 7), low coherence values, and background fluctuations. In Section 4.1, we obtained first order estimates of the amplitude and phase of seasonal variations, coseismic velocity reduction and post-seismic recovery time in various frequency bands. The estimated seasonal variations are later removed, and the highlighted co- and post-seismic $\delta v/v$ curves at different coda wave windows, frequency bands, components and arrays were analysed in Section 4.2.

For seasonal variations (Section 4.1.1), the observed $\delta v/v$ in the low-frequency band 0.1–0.4 Hz are likely spurious and governed by wavefield changes associated with annual variations in microseisms excitation. At higher frequencies between 0.5 and 4 Hz, the observed annual variations in $\delta v/v$ beneath the DW and JF arrays are comparable to those reported in Hillers et al. (2015a). The delay between the observed seasonal variations at these higher frequencies and the surface annual temperature record is ~40–100 d, suggesting thermoelastic strain is a possible primary mechanism. However, the phase delay, between the observed seasonal variations in $\delta v/v$ time-series and the assumed driving temperature changes, of the JF array are different from those of DW array, indicating effects of different local properties such as topography and fault zone structure.

The apparent coseismic velocity reduction is estimated to be ~6 and ~1 per cent at the DW and JF arrays, respectively, for the low frequency band 0.1–0.4 Hz and significantly smaller ~0.2 per cent for frequencies between 0.5 and 4 Hz (Fig. 5c). Assuming the depth sensitivity of coda waves to medium changes is the same as that of surface waves to shear wave velocity, observations at 0.1–0.4 Hz represent medium changes at a depth of $h_{\text{max}} = ~7–8$ km, whereas results at 1–4 Hz indicate perturbations in shallow materials, in the top 1–2 km. The ~12 km depth of the 2016 BS hypocentre is comparable to the $h_{\text{max}}$ estimate of ~7–8 km at 0.1–0.4 Hz. Hence the relatively large coseismic velocity reduction at the low frequency band (>1 per cent) implies that the corresponding driving mechanism is the rock damage associated with coseismic earthquake rupture. For frequencies above 0.5 Hz, the observed medium changes are much shallower and thus likely associated with the straining of the radiated waves.

The coseismic velocity changes are expected to be higher within the fault damage zone, that is underneath the array, than in the surrounding rock (Peng & Ben-Zion 2006). This is supported by the obtained negative correlation between coda lapse time and coseismic $\delta v/v$ reduction (Fig. 7; Section 4.2.1). As the coda wave sensitivity to velocity perturbations extends over larger regions at longer lapse time, the rate, $\eta$, at which coseismic $\delta v/v$ decreases with
coda lapse time \( t \), is likely indicative of the fault zone width, that is a faster decrease of coseismic \( \delta v/v \) indicates a narrower fault damage zone. At 0.1–0.4 Hz, the rate \( \eta \) is much higher at DW (Fig. 8a), whereas it is similar for both arrays at frequencies above 0.5 Hz (Fig. 8b), suggesting a narrower fault damage zone beneath site DW than JF at greater depth, and similar fault zone width at shallower depth. This is consistent with observations that fault zones in general and the SJFZ in particular have decreasing width with depth (e.g. Ben-Zion & Sammis 2003; Zigone et al. 2015), and differences in the imaged structures below the DW and JF arrays (Qiu et al. 2017a,b).

The localized coseismic velocity changes can also explain the observed large differences in the obtained coseismic velocity reduction \( E \) (eq. 4) between the stretching and doublet methods at 0.1–0.4 Hz (Section 4.1.2). Since the stretching method is performed in the time domain, the resulting coseismic \( \delta v/v \) is mainly governed by the velocity perturbation associated with the largest scattered arrival in the selected time window (Section 3.1), which is typically the arrival at the earlier lapse times (Fig. S3). The doublet method, on the other hand, is equivalent to a moving window cross-spectral analysis, in which \( \delta v/v \) is estimated through a linear regression of \( \delta t \) and \( t \). As \( \delta t \) measured at different lapse time \( t \) is equally weighted, lower \( \delta v/v \) values are expected for the doublet method, due to biases of smaller \( \delta t/\delta t \) at larger \( t \). In addition, we find the largest discrepancy in coseismic \( \delta v/v \) between the two methods at 0.1–0.4 Hz from the DW array data (Fig. 5c). This is consistent with the observation that the highest rate \( \eta \) is also seen at the 0.1–0.4 Hz band at the DW array (Fig. 8).

To separate effects of the loadings from the local rock susceptibility, we normalize the observed \( \delta v/v \) time-series by the amplitude of seasonal variations (Section 4.2.4). Systematically larger coseismic velocity reductions are observed at the DW site compared to the JF site (Figs 11 and S19), which can be explained by the asymmetrical distribution of coseismic slip and wave excitation associated with the NW rupture directivity of the 2016 BS earthquake (Ross et al. 2017). This suggests that the observed coseismic velocity reduction obtained from noise-based seismic monitoring resolve directivity effects of the earthquake rupture.

Amplitude values of the \( \delta v/v \) time-series estimates are sensitive to the various parameter and processing choices included in the analysis, such as window sizes, filter characteristics, normalization strategies, reference time period and details of the delay-change estimators such as the moving window size in the doublet method. Although the amplitude values of the annual variations and of the coseismic velocity reduction can vary depending on the method and implementation used to estimate \( \delta v/v \), we emphasize that our conclusions focus on systematic variations of relative amplitude changes between the DW and JF sites obtained with a consistent set of processing parameters applied to data from both sites.

For the post-seismic process, logarithmic recovery with time is commonly observed for timescales from seconds to months after material failure in laboratory experiments (e.g. Dieterich & Kilgore 1996; Nakatani & Scholz 2004; Johnson & Jia 2005) and earthquakes (e.g. Brenguier et al. 2008a; Wu et al. 2009, 2010). Such recovery processes have been related to healing of coseismic fractures, motion of fluids and post-seismic stress relaxation (e.g. Ben-Zion 2008; Roux & Ben-Zion 2013; Aben et al. 2017; Pei et al. 2019). Better understanding of the recovery time for fault zone rocks after an earthquake provides important constraints on fault strength and mechanics, and may influence various key issues ranging from long-term coupled evolution of earthquakes and faults (e.g. Ben-Zion et al. 1999; Lyakhovsky et al. 2001) to estimation of recurrence times of earthquakes (Gratier & Gueydan 2007).

In Section 4.1.3, the post-seismic recovery process is first characterized by an exponential function with effective recovery time parameter \( T_c \), (eq. 4b). We find significantly smaller \( T_c \) values (~10 d) at 0.1–0.4 Hz than those (>100 d) at 0.5–4 Hz (Fig. 5c). This is related to the normal stress increase with depth, as lower frequency coda waves are more sensitivity to changes in deeper structures and faster healing with larger normal stress. The \( T_c \) values of DW array at frequencies above 0.5 Hz are larger than those of JF array, suggesting a slower post-seismic healing process in the medium below DW that is likely related to local structures, such as fault zone rheology. In Figs 6 and S15, we validate that compatible recovery time \( T_{re} \) is obtained when using a logarithmic function (eq. 3) to fit the post-seismic section of the \( \delta v/v \) time-series. Moreover, the results in the 0.1–0.4 Hz band indicate that the \( E \) value obtained for DW array (~6 per cent in Fig. 5c) likely underestimates the actual coseismic velocity reduction due to the lack of resolution in the first 2 weeks after the BS event (Section 3.2). The refined analysis (Fig. 6a) suggests a significantly larger coseismic velocity reduction (\( E_{re} \approx 36 \) per cent) followed by a rapid recovery at 0.1–0.4 Hz for DW array. This is expected as the medium changes indicated by this low frequency band at DW array is likely associated with rock damage produced by the coseismic slip at greater depth (grey shaded area in Fig. 1b) where normal stress is high.

The lapse time analysis demonstrated in Section 4.2.1 shows results that can be understood from the outcomes of 3-D wavefield simulations conducted by Obermann et al. (2016). However, full quantification requires further wavefield simulations using models that better characterize the fault zone structures and station configurations at DW and JF. In addition to the velocity changes associated with the discussed thermoelastic strain and the 2016 BS event, other external loading mechanisms such as solid Earth tides (Hillers & Campillo 2016) provide further possibilities for recovery time analysis. All previous noise-based monitoring studies of seismic velocity zone arrays at the opposite along-strike directions from the epicentre. The results of the study can potentially be improved by applying more refined corrections of seasonal and environmental effects using meteorological and oceanographic data (Wang et al. 2017). The results resolve for the first time the response of fault damage zone to a nearby earthquake rupture using data from two linear fault zone arrays at the opposite along-strike directions from the epicentre. All previous noise-based monitoring studies of seismic velocity changes associated with earthquakes resolved the response of the medium adjacent to or surrounding the fault, but not within the fault damage zone. Monitoring processes in damage zones is challenging because of their spatially localized structures with low elastic moduli and high rock susceptibility, which is difficult to resolve using noise-based coda wave analysis. Monitoring the properties of fault zone trapped noise and reconstructed trapped modes (Hillers et al. 2014; Hillers & Campillo 2016) provide further possibilities for in situ fault zone studies.
REFERENCES


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**SUPPORTING INFORMATION**

Supplementary data are available at *GJI* online.

**Figure S1.** Magnitude-time distribution (black dots) of the seismicity that occurred within the trucification area of the SJFZ shown in Fig. 1 for the period 2 d before and 15 d after the occurrence time of the 2016 BS earthquake. The beach ball indicates the focal mechanism of the main shock. Red stars denote aftershocks with $M_n > 3.0$. The daily frequency of seismicity is shown in the blue.

**Figure S2.** Same as Fig. 2 for raw daily cross correlations. Low quality daily correlations are found and removed in a two-step process. First, we remove outliers based on the median absolute deviation (MAD) of the maximum absolute amplitudes of all daily ANC. Correlation functions with maximum amplitudes three times smaller or four times larger than the MAD from the median are removed. Second, we construct a reference signal by stacking all daily ANC, and identify outliers through the correlation coefficient of the reference and each daily traces. Since the central peak between lag times of $\pm 1$ s ($|\tau| < 1$s) dominate the correlation, we first truncate the near-zero peak within the window of $|\tau| < 1$s and then cross correlate waveforms between lag times of $\pm 60$s. Daily correlations are discarded if the maximum cross-correlation coefficient is smaller than 0.5.

**Figure S3.** (a) Reference waveform (blue) and the corresponding envelope function (black, in log scale) averaged over all station pairs in DW and JF arrays filtered at 0.1–0.4 Hz for ZZ component. The correlation is fold and averaged. Envelope function of each symmetric correlation at individual station pair is shown in grey. The green dashed curves represent the best-fitting amplitude decay from 0 to 60 s that is governed by geometrical spreading and attenuation, whereas the red dashed lines depicted the best-fitting decay from 6 to 40 s that is only affected by intrinsic and scattering attenuation. The black dashed lines outline the coda wave window (i.e. 6–40 s). Here, we truncate the window at the lapse time of 40 s to ensure sufficient signal to noise ratio. Coda waves between 6 and 40 s are magnified and shown in red. (b) Same as for (a) for frequency band 0.5–2 Hz. The resulting coda wave window is 8–35 s. (c) Same as (a) for frequency band 0.75–3 Hz with the corresponding coda wave window as 6–23 s. (d) Same as (a) for frequency band 1–4 Hz with the coda wave window as 5–22 s.

**Figure S4.** Same as Fig. S3(a) for frequency band 0.25–1 Hz. We do not include this frequency band due to insufficient SNR.

**Figure S5.** Coda waves between lapse time 8 and 15 s at both negative (a) and positive (b) lags for a 120-d period centred on the occurrence time of the 2016 BS event (red dashed lines) bandpass filtered at 0.1–0.4 Hz. The scattered arrivals reconstructed from the ANC are fairly symmetrical. (c), (d), same as (a), (b) but for a 60-d period and frequency band 0.5–2 Hz. The coda waves are highly asymmetric. (e), (f), same as (c), (d) for frequency band 1–4 Hz. Coherent scattered arrivals are observed throughout the time period for all three frequency bands.

**Figure S6.** Same as Fig. 3 but for 0.1–0.4 Hz using a coda wave window of 8–40s. Different from Fig. 3, large periodic fluctuations (~6 per cent peak to peak variation and ~40-d periodicity) in $\delta v/v$ is observed between May and October in 2015.

**Figure S7.** Same as Fig. 3 but for 0.5–2 Hz and using a coda wave window of 8–25 s.

**Figure S8.** Same as Fig. 3 but for 0.75–3 Hz and using a coda wave window of 6–23 s.

**Figure S9.** (a) Synthetic co- and post-seismic $\delta v/v$ curves calculated using eq. (3) for a selection of $E_1/E_2$ values. (b) Synthetic co- and post-seismic velocity changes predicted using eq. (4a).

**Figure S10.** Same as Fig. 4 for results using doublet method. Although the amplitudes of seasonal and coseismic components are smaller compared to those using stretching method, the temporal patterns are similar regardless of the method used.

**Figure S11.** Same as Fig. 4 for JF array.

**Figure S12.** Same as Fig. S11 for results using doublet method.

**Figure S13.** (a) Same as Fig. 7(a) before removing the long term variations including a linear trend, annual and semi-annual variations. (b) Same as (a) but for JF array. (c), (d) Same as (a), (b) for frequency band 0.5–2 Hz. A very high consistency in seasonal variations is observed for all lapse time windows. Same observations are seen in results from doublet method (not shown here).
Figure S14. Same as Fig. S13 for frequency bands (a), (b) 0.75–3 Hz and (c), (d) 1–4 Hz. Almost the same seasonal variation is observed for all lapse time windows. Same observations are seen in results from doublet method (not shown here).

Figure S15. Same as Fig. 6 for stretching method-based results at (a) DW array in 0.5–2 Hz, (b) DW array in 0.75–3 Hz, (c) DW array in 1–4 Hz, (d) JF array in 0.5–2 Hz, (e) JF array in 0.75–3 Hz and (f) JF array in 1–4 Hz. Different post-seismic time windows, $T > T_0 + 14$ (red dashed lines), $T > T_0 + 5$ (black dashed lines) and $T_0 + 14 < T < T_0 + 100$ (grey dashed lines), are used in (a)–(c) to provide estimates of coseismic velocity reduction $E_{log}$ and post-seismic recovery time $T_{log}$, illustrated by the red line, black triangles and grey circles, respectively.

Figure S16. Same as Fig. 10 using the doublet method. Here only results for components ZZ (vertical-vertical in black), RR (fault parallel – fault parallel in blue) and TT (fault normal – fault normal in red) are shown.

Figure S17. Same as Fig. 10 for the JF array.

Figure S18. Same as Fig. S16 for doublet method.

Figure S19. Same as Fig. 11 for the frequency band 0.1–0.4 Hz.

Figure S20. Same as Fig. 11 for the frequency band 0.5–2 Hz.

Figure S21. Same as Fig. 11 for the frequency band 0.75–3 Hz.

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